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# Is There a Dispersion of the Dielectric Constant of Material Media

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**Abstract**

By all is well known this phenomenon as rainbow. To any specialist in the electrodynamics it is clear that the appearance of rainbow is connected with the dependence on the frequency of the phase speed of the electromagnetic waves, passing through the drops of rain. Since water is dielectric, with the explanation of this phenomenon J. Heaviside R. Vul assumed that this dispersion was connected with the frequency dispersion (dependence on the frequency) of the dielectric constant of water. Since then this point of view is ruling. However, this approach is physical and methodological error, that also is shown in this article. This error occurred because of the fact that during the record of current in the material media they were entangled integral and the derivative of the harmonic function, which take the identical form and are characterized by only signs.

**1. Introduction**

By all is well known this phenomenon as rainbow. To any specialist in the electrodynamics it is clear that the appearance of rainbow is connected with the dependence on the frequency of the phase speed of the electromagnetic waves, passing through the drops of rain. Since water is dielectric, with the explanation of this phenomenon J. Heaviside R. Vul assumed that this dispersion was connected with the frequency dispersion (dependence on the frequency) of the dielectric constant of water. Since then this point of view is ruling [1-6].

However very creator of the fundamental equations of electrodynamics Maxwell considered that these parameters on frequency do not depend, but they are fundamental constants. As the idea of the dispersion of dielectric and magnetic constant was born, and what way it was past, sufficiently colorfully characterizes quotation from the monograph of well well-known specialists in the field of physics of plasma [1]: "J. itself. Maxwell with the formulation of the equations of the electrodynamics of material media considered that the dielectric and magnetic constants are the constants (for this reason they long time they were considered as the constants). It is considerably later, already at the beginning of this century with the explanation of the optical dispersion phenomena (in particular the phenomenon of rainbow) J. Heaviside R. Vul showed that the dielectric and magnetic constants are the functions of frequency. But very recently, in the middle of the 50's, physics they came to the conclusion that these values depend not only on frequency, but also on the wave vector. On the essence, this was the radical breaking of the existing ideas. It was how a serious, is characterized the case, which occurred at the seminar L. D. Landau into 1954 during the report of A. I. Akhiezer on this theme of Landau suddenly exclaimed, after smashing the speaker: "This is delirium, since the refractive index cannot be the function of refractive index". Note that this said L. D. Landau - one of the outstanding physicists of our time" (end of the quotation).

It is incomprehensible from the given quotation, that precisely had in the form Landau. However, its subsequent publications speak, that it accepted this concept [2].

That rights there was Maxwell, who considered that the dielectric and magnetic constant of material media on frequency they do not depend. However, in a number of fundamental works on electrodynamics [2-6] are committed conceptual, systematic and physical errors, as a result of which in physics they penetrated and solidly in it were fastened such metaphysical concepts as the frequency dispersion of the dielectric constant of material media and, in particular, plasma. The propagation of this concept to the dielectrics led to the fact that all began to consider that also the dielectric constant of dielectrics also depends on frequency. These physical errors penetrated in all spheres of physics and technology. They so solidly took root in the consciousness of specialists, that many, until now, cannot believe in the fact that the dielectric constant of plasma is equal to the dielectric constant of vacuum, but the dispersion of the dielectric constant of dielectrics is absent. There is the publications of such well-known scholars as the Drudes, Vull, Heaviside, Landau, Ginsburg, Akhiezer, Tamm [1-6], where it is indicated that the dielectric constant of plasma and dielectrics depends on frequency. This is a systematic and physical error. This systematic and physical error became possible for that reason, that without the proper understanding of physics of the proceeding processes occurred the substitution of physical concepts by mathematical symbols, which appropriated physical, but are more accurate metaphysical, designations, which do not correspond to their physical sense. But if we examine the purely mathematical point of view, then Landau, and following it and other authors entangled integral and derivative of harmonic function, since they forgot, that the derivative and integral in this case take the identical form, and they are characterized by only signs.

## 2. Plasmo-Like Media

By plasma media we will understand such, in which the charges can move without the losses. To such media in the first approximation, can be related the superconductors, free electrons or ions in the vacuum (subsequently conductors). In the absence magnetic field in the media indicated equation of motion for the electrons takes the form:

$$m \frac{d\vec{v}}{dt} = e\vec{E}, \quad (2.1)$$

where  $m$  is the mass electron,  $e$  is the electron charge,  $\vec{E}$  is the tension of electric field,  $\vec{v}$  is the speed of the motion of charge.

In the work [6] it is shown that this equation can be used also for describing the electron motion in the hot plasma. Therefore it can be disseminated also to this case.

Using an expression for the current density

$$\vec{j} = ne\vec{v}, \quad (2.2)$$

from (2.1) we obtain the current density of the conductivity

$$\vec{j}_L = \frac{ne^2}{m} \int \vec{E} dt. \quad (2.3)$$

In relationship (2.2) and (2.3) the value  $n$  represents electron density. After introducing the designation

$$L_k = \frac{m}{ne^2}, \quad (2.4)$$

we find

$$\vec{j}_L = \frac{1}{L_k} \int \vec{E} dt. \quad (2.5)$$

In this case the value  $L_k$  presents the specific kinetic inductance of charge carriers [7-11]. Its existence connected with the fact that charge, having a mass, possesses inertia properties. Field on  $\vec{E} = \vec{E}_0 \sin \omega t$  relationship (2.5) it will be written down for the case of harmonics:

$$\vec{j}_L = -\frac{1}{\omega L_k} \vec{E}_0 \cos \omega t. \quad (2.6)$$

For the mathematical description of electrodynamic processes the trigonometric functions will be here and throughout, instead of the complex quantities, used so that would be well visible the phase relationships between the vectors, which represent electric fields and current densities.

From relationship (2.5) and (2.6) is evident that  $\vec{j}_L$  presents inductive current, since. its phase is late with respect to the tension of electric field to the angle  $\frac{\pi}{2}$ .

If charges are located in the vacuum, then during the presence of summed current it is necessary to consider bias current

$$\vec{j}_\epsilon = \epsilon_0 \frac{\partial \vec{E}}{\partial t} = \epsilon_0 \vec{E}_0 \cos \omega t.$$

Is evident that this current bears capacitive nature, since its phase anticipates the phase of the tension of electrical field to the angle  $\frac{\pi}{2}$ . Thus, summary current density will compose [8-10]

$$\vec{j}_\Sigma = \epsilon_0 \frac{\partial \vec{E}}{\partial t} + \frac{1}{L_k} \int \vec{E} dt,$$

or

$$\vec{j}_{\Sigma} = \left( \omega \epsilon_0 - \frac{1}{\omega L_k} \right) \vec{E}_0 \cos \omega t. \quad (2.7)$$

If electrons are located in the material medium, then should be considered the presence of the positively charged ions. However, with the examination of the properties of such media in the rapidly changing fields, in connection with the fact that the mass of ions is considerably more than the mass of electrons, their presence usually is not considered.

In relationship (2.7) the value, which stands in the brackets, presents summary susceptance of this medium  $\sigma_{\Sigma}$  and it consists it, in turn, of the the capacitive  $\sigma_C$  and by the inductive  $\sigma_L$  the conductivity

$$\sigma_{\Sigma} = \sigma_C + \sigma_L = \omega \epsilon_0 - \frac{1}{\omega L_k}.$$

Relationship (2.7) can be rewritten and differently:

$$\vec{j}_{\Sigma} = \omega \epsilon_0 \left( 1 - \frac{\omega_0^2}{\omega^2} \right) \vec{E}_0 \cos \omega t,$$

where  $\omega_0 = \sqrt{\frac{1}{L_k \epsilon_0}}$  is plasma frequency.

And large temptation here appears to name the value

$$\epsilon^*(\omega) = \epsilon_0 \left( 1 - \frac{\omega_0^2}{\omega^2} \right) = \epsilon_0 - \frac{1}{\omega^2 L_k},$$

by the depending on the frequency dielectric constant of plasma, that also is made in all existing works on physics of plasma. But this is incorrect, since. this mathematical symbol is the composite parameter, into which simultaneously enters the dielectric constant of vacuum and the specific kinetic inductance of charges. It is clear from the previous examination that the parameter  $\epsilon^*(\omega)$  gives the possibility in one coefficient to combine derivative and the integral of harmonic function, since they are characterized by only signs and thus impression is created, that the dielectric constant of plasma depends on frequency. It should be noted that a similar error is perfected by such well-known physicists as Akhiezer, Tamm, Ginsburg [3-5].

This happened still and because, beginning to examine this question, Landau introduced the determinations of dielectric constant only for the static fields on, but he did not introduce this determination for the variables fields on. Let us introduce this determination.

If we examine any medium, including plasma, then current density (subsequently we will in abbreviated form speak simply current) it will be determined by three components, which depend on the electric field. The current of resistance losses there will be sinphase to electric field. The permittance current, determined by first-order derivative of electric field from the time, will anticipate the tension of electric field on

the phase to  $\frac{\pi}{2}$ . This current is called bias current. The

conduction current, determined by integral of the electric field from the time, will lag behind the electric field on the phase to

$\frac{\pi}{2}$ . All three components of current indicated will enter into

the second equation of Maxwell and others components of currents be it cannot. Moreover all these three components of currents will be present in any nonmagnetic regions, in which there are losses. Therefore it is completely natural, the dielectric constant of any medium to define as the coefficient, confronting that term, which is determined by the derivative of electric field by the time in the second equation of Maxwell. In this case one should consider that the dielectric constant cannot be negative value. This connected with the fact that through this parameter is determined energy of electrical fields on, which can be only positive.

Without having introduced this clear determination of dielectric constant, Landau begins the examination of the behavior of plasma in the ac fields. In this case is not separated separately the bias current and conduction current, one of which is defined by derivative, but by another integral, is written as united bias current. It makes this error for that reason, that in the case of harmonic oscillations the form of the function, which determine and derivative and integral, is identical, and they are characterized by only sign. Performing this operation, Landau does not understand, that in the case of harmonic electrical fields on in the plasma there exist two different currents, one of which is bias current, and it is determined by the dielectric constant of vacuum and derivative of electric field. Another current is conduction current and is determined by integral of the electric field. These two currents are antiphase. But since both currents depend on frequency, moreover one of them depends on frequency linearly, and another it is inversely proportional to frequency, between them competition occurs. The conduction current predominates with the low frequencies, the bias current, on the contrary, predominates with the high. However, in the case of the equality of these currents, which occurs at the plasma frequency, occurs current resonance.

Let us emphasize that from a mathematical point of view to reach in the manner that it entered to Landau, it is possible, but in this case is lost the integration constant, which is necessary to account for initial conditions during the solution of the equation, which determines current density in the material medium.

The obviousness of the committed error is visible based on other example.

Relationship (2.7) can be rewritten and differently:

$$\vec{j}_{\Sigma} = - \frac{\left( \frac{\omega^2}{\omega_0^2} - 1 \right)}{\omega L} \vec{E}_0 \cos \omega t$$

and to introduce another mathematical symbol

$$L^*(\omega) = \frac{L_k}{\left(\frac{\omega^2}{\omega_0^2} - 1\right)} = \frac{L_k}{\omega^2 L_k \varepsilon_0 - 1}.$$

$$W = \frac{1}{2} \frac{d \left[ \frac{1}{\omega L_k^*(\omega)} \right]}{d\omega} E_0^2.$$

In this case also appears temptation to name this bending coefficient on the frequency kinetic inductance.

Thus, it is possible to write down:

$$\vec{j}_\Sigma = \omega \varepsilon^*(\omega) \vec{E}_0 \cos \omega t,$$

or

$$\vec{j}_\Sigma = -\frac{1}{\omega L^*(\omega)} \vec{E}_0 \cos \omega t.$$

But this altogether only the symbolic mathematical record of one and the same relationship (2.7). Both equations are equivalent. But view neither  $\varepsilon^*(\omega)$  nor  $L^*(\omega)$  by dielectric constant or inductance are from a physical point. The physical sense of their names consists of the following:

$$\varepsilon^*(\omega) = \frac{\sigma_X}{\omega},$$

i.e.  $\varepsilon^*(\omega)$  presents summary susceptance of medium, divided into the frequency, and

$$L_k^*(\omega) = \frac{1}{\omega \sigma_X}$$

it represents the reciprocal value of the work of frequency and susceptance of medium.

As it is necessary to enter, if at our disposal are values  $\varepsilon^*(\omega)$  and  $L^*(\omega)$ , and we should calculate total specific energy? Natural to substitute these values in the formulas, which determine energy of electrical fields

$$W_E = \frac{1}{2} \varepsilon_0 E_0^2$$

and kinetic energy of charge carriers

$$W_j = \frac{1}{2} L_k j_0^2, \quad (2.8)$$

is cannot simply because these parameters are neither dielectric constant nor inductance. It is not difficult to show that in this case the total specific energy can be obtained from the relationship

$$W_\Sigma = \frac{1}{2} \cdot \frac{d(\omega \varepsilon^*(\omega))}{d\omega} E_0^2, \quad (2.9)$$

from where we obtain

$$W_\Sigma = \frac{1}{2} \varepsilon_0 E_0^2 + \frac{1}{2} \frac{1}{\omega^2 L_k} E_0^2 = \frac{1}{2} \varepsilon_0 E_0^2 + \frac{1}{2} L_k j_0^2.$$

We will obtain the same result, after using the formula

The given relationships show that the specific energy consists of potential energy of electrical fields on and to kinetic energy of charge carriers.

With the examination of any media by our final task appears the presence of wave equation. In this case this problem is already practically solved. Maxwell's equations for this case take the form:

$$\begin{aligned} \text{rot } \vec{E} &= -\mu_0 \frac{\partial \vec{H}}{\partial t}, \\ \text{rot } \vec{H} &= \varepsilon_0 \frac{\partial \vec{E}}{\partial t} + \frac{1}{L_k} \int \vec{E} dt, \end{aligned} \quad (2.10)$$

where  $\varepsilon_0$ ,  $\mu_0$  are dielectric and magnetic constant of vacuum.

The system of equations (2.10) completely describes all properties of nondissipative conductors. From it we obtain

$$\text{rot rot } \vec{H} + \mu_0 \varepsilon_0 \frac{\partial^2 \vec{H}}{\partial t^2} + \frac{\mu_0}{L_k} \vec{H} = 0 \quad (2.11)$$

For the case fields on, time-independent, equation (2.11) passes into the equation of London

$$\text{rot rot } \vec{H} + \frac{\mu_0}{L_k} \vec{H} = 0,$$

where  $\lambda_L^2 = \frac{L_k}{\mu_0}$  is London depth of penetration.

Thus, it is possible to conclude that the equations of London being a special case of equation (2.11), and do not consider bias currents on medium. Therefore they do not give the possibility to obtain the wave equations, which describe the processes of the propagation of electromagnetic waves in the superconductors.

Fields on wave equation in this case it appears as follows for the electrical:

$$\text{rot rot } \vec{E} + \mu_0 \varepsilon_0 \frac{\partial^2 \vec{E}}{\partial t^2} + \frac{\mu_0}{L_k} \vec{E} = 0.$$

For constant electrical fields on it is possible to write down

$$\text{rot rot } \vec{E} + \frac{\mu_0}{L_k} \vec{E} = 0.$$

Consequently, dc fields penetrate the superconductor in the same manner as for magnetic, diminishing exponentially. However, the density of current in this case grows according to the linear law

$$\vec{j}_L = \frac{1}{L_k} \int \vec{E} dt .$$

The carried out examination showed that the dielectric constant of this medium was equal to the dielectric constant of vacuum and this permeability on frequency does not depend. The accumulation of potential energy is obliged to this parameter. Furthermore, this medium is characterized still and the kinetic inductance of charge carriers and this parameter determines the kinetic energy, accumulated on medium.

Thus, are obtained all necessary given, which characterize the process of the propagation of electromagnetic waves in conducting media examined. However, in contrast to the conventional procedure [2-4] with this examination nowhere was introduced polarization vector, but as the basis of examination assumed equation of motion and in this case in the second equation of Maxwell are extracted all components of current densities explicitly.

In radio engineering exists the simple method of the idea of radio-technical elements with the aid of the equivalent diagrams. This method is very visual and gives the possibility to present in the form such diagrams elements both with that concentrated and with the distributed parameters. The use of this method will make it possible better to understand, why were committed such significant physical errors during the introduction of the concept of that depending on the frequency dielectric constant.

In order to show that the single volume of conductor or plasma according to its electrodynamic characteristics is equivalent to parallel resonant circuit with the lumped parameters, let us examine parallel resonant circuit. The connection between the voltage  $U$ , applied to the outline, and the summed current  $I_\Sigma$ , which flows through this chain, takes the form

$$I_\Sigma = I_C + I_L = C \frac{dU}{dt} + \frac{1}{L} \int U dt ,$$

where  $I_C = C \frac{dU}{dt}$  is current, which flows through the capacity, and  $I_L = \frac{1}{L} \int U dt$  is current, which flows through the inductance.

For the case of the harmonic stress of  $U = U_0 \sin \omega t$  we obtain

$$I_\Sigma = \left( \omega C - \frac{1}{\omega L} \right) U_0 \cos \omega t \tag{2.12}$$

In relationship (2.12) the value, which stands in the brackets, presents summary susceptance  $\sigma_\Sigma$  this medium and it consists it, in turn, of the the capacitive  $\sigma_C$  and by the inductive  $\sigma_L$  the conductivity

$$\sigma_\Sigma = \sigma_C + \sigma_L = \omega C - \frac{1}{\omega L} .$$

In this case relationship (2.12) can be rewritten as follows:

$$I_\Sigma = \omega C \left( 1 - \frac{\omega_0^2}{\omega^2} \right) U_0 \cos \omega t ,$$

where  $\omega_0^2 = \frac{1}{LC}$  is the resonance frequency of parallel circuit.

And here, just as in the case of conductors, appears temptation, to name the value

$$C^*(\omega) = C \left( 1 - \frac{\omega_0^2}{\omega^2} \right) = C - \frac{1}{\omega^2 L} \tag{2.13}$$

by the depending on the frequency capacity. Conducting this symbol it is permissible from a mathematical point of view; however, inadmissible is awarding to it the proposed name, since. this parameter of no relation to the true capacity has and includes in itself simultaneously and capacity and the inductance of outline, which do not depend on frequency.

Is accurate another point of view. Relationship (2.12) can be rewritten and differently:

$$I_\Sigma = - \frac{\left( \frac{\omega^2}{\omega_0^2} - 1 \right)}{\omega L} U_0 \cos \omega t ,$$

and to consider that the chain in question not at all has capacities, and consists only of the inductance depending on the frequency

$$L^*(\omega) = \frac{L}{\left( \frac{\omega^2}{\omega_0^2} - 1 \right)} = \frac{L}{\omega^2 LC - 1} \tag{2.14}$$

But, just as  $C^*(\omega)$ , the value of  $L^*(\omega)$  cannot be called inductance, since this is the also composite parameter, which includes simultaneously capacity and inductance, which do not depend on frequency.

Using expressions (2.13) and (2.14), let us write down:

$$I_\Sigma = \omega C^*(\omega) U_0 \cos \omega t , \tag{2.15}$$

or

$$I_\Sigma = - \frac{1}{\omega L^*(\omega)} U_0 \cos \omega t . \tag{2.16}$$

The relationship (2.15) and (2.16) are equivalent, and separately mathematically completely is characterized the chain examined. But view neither  $C^*(\omega)$  nor  $L^*(\omega)$  by capacity and inductance are from a physical point, although they have the same dimensionality. The physical sense of their names consists of the following:

$$C^*(\omega) = \frac{\sigma_x}{\omega} ,$$

i.e.  $C^*(\omega)$  presents the relation of susceptance of this chain and frequency, and

$$L^*(\omega) = \frac{1}{\omega\sigma_x},$$

it is the reciprocal value of the work of summary susceptance and frequency.

Accumulated in the capacity and the inductance energy, is determined from the relationships

$$W_C = \frac{1}{2}CU_0^2 \tag{2.17}$$

$$W_L = \frac{1}{2}LI_0^2. \tag{2.18}$$

How one should enter for enumerating the energy, which was accumulated in the outline, if at our disposal are  $C^*(\omega)$  and  $L^*(\omega)$ ? Certainly, to put these relationships in formulas (2.17) and (2.18) cannot for that reason, that these values can be both the positive and negative, and the energy, accumulated in the capacity and the inductance, is always positive. But if we for these purposes use ourselves the parameters indicated, then it is not difficult to show that the summary energy, accumulated in the outline, is determined by the expressions:

$$W_\Sigma = \frac{1}{2} \frac{d\sigma_x}{d\omega} U_0^2, \tag{2.19}$$

or

$$W_\Sigma = \frac{1}{2} \frac{d[\omega C^*(\omega)]}{d\omega} U_0^2, \tag{2.20}$$

or

$$W_\Sigma = \frac{1}{2} \frac{d\left(\frac{1}{\omega L^*(\omega)}\right)}{d\omega} U_0^2. \tag{2.21}$$

If we paint equations (2.19) or (2.20) and (2.21), then we will obtain identical result, namely:

$$W_\Sigma = \frac{1}{2}CU_0^2 + \frac{1}{2}LI_0^2,$$

where  $U_0$  is amplitude of voltage on the capacity, and  $I_0$  is amplitude of the current, which flows through the inductance.

If we compare the relationships, obtained for the parallel resonant circuit and for the conductors, then it is possible to see that they are identical, if we make  $E_0 \rightarrow U_0$ ,  $j_0 \rightarrow I_0$ ,  $\epsilon_0 \rightarrow C$  and  $L_k \rightarrow L$ . Thus, the single volume of conductor, with the uniform distribution of electrical fields on and current densities in it, it is equivalent to parallel resonant circuit with the lumped parameters indicated. In this case the capacity of this outline is numerically equal to the dielectric constant of vacuum, and inductance is equal to the specific kinetic

inductance of charges.

Now let us visualize this situation. In the audience, where are located specialists, who know radio engineering and of mathematics, comes instructor and he begins to prove, that there are in nature of no capacities and inductances, and there is only depending on the frequency capacity and that just she presents parallel resonant circuit. Or, on the contrary, that parallel resonant circuit this is the depending on the frequency inductance. View of mathematics will agree from this point. However, radio engineering they will calculate lecturer by man with the very limited knowledge. Specifically, in this position proved to be now those scientists and the specialists, who introduced into physics the frequency dispersion of dielectric constant.

Thus, are obtained all necessary given, which characterize the process of the propagation of electromagnetic waves in the media examined, and it is also shown that in the quasi-static regime the electrodynamic processes in the conductors are similar to processes in the parallel resonant circuit with the lumped parameters. However, in contrast to the conventional procedure [2-5] with this examination nowhere was introduced polarization vector, but as the basis of examination assumed equation of motion and in this case in the second equation of Maxwell are extracted all components of current densities explicitly.

Based on the example of work [2] let us examine a question about how similar problems, when the concept of polarization vector is introduced are solved for their solution. Paragraph 59 of this work, where this question is examined, it begins with the words: "We pass now to the study of the most important question about the rapidly changing electric fields, whose frequencies are unconfined by the condition of smallness in comparison with the frequencies, characteristic for establishing the electrical and magnetic polarization of substance" (end of the quotation). These words mean that that region of the frequencies, where, in connection with the presence of the inertia properties of charge carriers, the polarization of substance will not reach its static values, is examined. With the further consideration of a question is done the conclusion that "in any variable field, including with the presence of dispersion, the polarization vector  $\vec{P} = \vec{D} - \epsilon_0\vec{E}$  (here and throughout all formulas cited they are written in the system SI) preserves its physical sense of the electric moment of the unit volume of substance" (end of the quotation). Let us give the still one quotation: "It proves to be possible to establish (unimportantly - metals or dielectrics) maximum form of the function  $\epsilon(\omega)$  with the high frequencies valid for any bodies. Specifically, the field frequency must be great in comparison with "the frequencies" of the motion of all (or, at least, majority) electrons in the atoms of this substance. With the observance of this condition it is possible with the calculation of the polarization of substance to consider electrons as free, disregarding their interaction with each other and with the atomic nuclei" (end of the quotation).

Further, as this is done and in this work, is written the equation of motion of free electron in the ac field

$$m \frac{d\vec{v}}{dt} = e\vec{E},$$

from where its displacement is located

$$\vec{r} = -\frac{e\vec{E}}{m\omega^2}.$$

Then is indicated that the polarization  $\vec{P}$  is a dipole moment of unit volume and the obtained displacement is put into the polarization

$$\vec{P} = ne\vec{r} = -\frac{ne^2\vec{E}}{m\omega^2}.$$

In this case point charge is examined, and this operation indicates the introduction of electrical dipole moment for two point charges with the opposite signs, located at a distance  $\vec{r}$

$$\vec{p}_e = -e\vec{r},$$

where the vector  $\vec{r}$  is directed from the negative charge toward the positive charge. This step causes bewilderment, since the point electron is examined, and in order to speak about the electrical dipole moment, it is necessary to have in this medium for each electron another charge of opposite sign, referred from it to the distance  $\vec{r}$ . In this case is examined the gas of free electrons, in which there are no charges of opposite signs. Further follows the standard procedure, when introduced thus illegal polarization vector is introduced into the dielectric constant

$$\vec{D} = \epsilon_0\vec{E} + \vec{P} = \epsilon_0\vec{E} - \frac{ne^2\vec{E}}{m\omega^2} = \epsilon_0 \left( 1 - \frac{1}{\epsilon_0 L_k \omega^2} \right) \vec{E},$$

and since plasma frequency is determined by the relationship

$$\omega_p^2 = \frac{1}{\epsilon_0 L_k},$$

the vector of the induction immediately is written

$$\vec{D} = \epsilon_0 \left( 1 - \frac{\omega_p^2}{\omega^2} \right) \vec{E}.$$

With this approach it turns out that constant of proportionality

$$\epsilon(\omega) = \epsilon_0 \left( 1 - \frac{\omega_p^2}{\omega^2} \right),$$

between the electric field and the electrical induction, illegally named dielectric constant, depends on frequency.

Precisely this approach led to the fact that all began to consider that the value, which stands in this relationship before the vector of electric field, is the dielectric constant depending on the frequency, and electrical induction also depends on frequency. And this it is discussed in all, without

the exception, fundamental works on the electrodynamics of material media [2-6].

But, as it was shown above this parameter it is not dielectric constant, but presents summary susceptance of medium, divided into the frequency. Thus, traditional approach to the solution of this problem from a physical point of view is erroneous, although formally this approach is permitted from a mathematical point of view, with this do not to consider initial conditions with the calculation of integral in the relationships, which determine conduction current.

Further into §61 of work [2] is examined a question about the energy of electrical and magnetic field in the media, which possess by the so-called dispersion. In this case is done the conclusion that relationship for the energy of such fields

$$W = \frac{1}{2} (\epsilon E_0^2 + \mu H_0^2), \tag{2.22}$$

that making precise thermodynamic sense in the usual media, with the presence of dispersion so interpreted be cannot. These words mean that the knowledge of real electrical and magnetic fields on medium with the dispersion insufficiently for determining the difference in the internal energy per unit of volume of substance in the presence fields on in their absence. After such statements is given the formula, which gives correct result for enumerating the specific energy of electrical and magnetic fields on when the dispersion present

$$W = \frac{1}{2} \frac{d(\omega\epsilon(\omega))}{d\omega} E_0^2 + \frac{1}{2} \frac{d(\omega\mu(\omega))}{d\omega} H_0^2 \tag{2.23}$$

But if we compare the first part of the expression in the right side of relationship (2.23) with relationship (2.9), then it is evident that they coincide. This means that in relationship (2.23) this term presents the total energy, which includes not only potential energy of electrical fields on, but also kinetic energy of the moving charges. On what base is recorded last term in the relationship (2.23) not at all clearly.

Therefore conclusion about the impossibility of the interpretation of formula (2.22), as the internal energy of electrical and magnetic fields on in the media with the dispersion it is correct. However, this circumstance consists not in the fact that this interpretation in such media is generally impossible. It consists in the fact that for the definition of the value of specific energy as the thermodynamic parameter in this case is necessary to correctly calculate this energy, taking into account not only electric field, which accumulates potential energy, but also current of the conduction electrons, which accumulate the kinetic energy of charges (2.8). The conclusion, which now can be made, consists in the fact that, introducing into the custom some mathematical symbols, without understanding of their true physical sense, and, all the more, the awarding to these symbols of physical designations unusual to them, it is possible in the final analysis to lead to the significant errors, that also occurred in the work [2].

### 3. Transverse Plasma Resonance

Now let us show how the poor understanding of physics of processes in conducting media it led to the fact that proved to be unnoticed the interesting physical phenomenon transverse plasma resonance in the nonmagnetized plasma, which can have important technical appendices. This phenomenon can have important technical appendices [13].

Is known that the plasma resonance is longitudinal. But longitudinal resonance cannot emit transverse electromagnetic waves. However, with the explosions of nuclear charges, as a result of which is formed very hot plasma, occurs electromagnetic radiation in the very wide frequency band, up to the long-wave radio-frequency band. Today are not known those of the physical mechanisms, which could explain the appearance of this emission. On existence in the nonmagnetized plasma of any other resonances, except Langmuir, earlier known it was not, but it occurs that in the confined plasma the transverse resonance can exist, and the frequency of this resonance coincides with the frequency of Langmuir resonance, i.e., these resonance are degenerate. Specifically, this resonance can be the reason for radio-wave emission with the explosions of nuclear charges, since the cloud of explosion in the process of its development for a while remains limited. For explaining the conditions for the excitation of this resonance let us examine the long line, which consists of two ideally conducting planes, as shown in Fig 1.

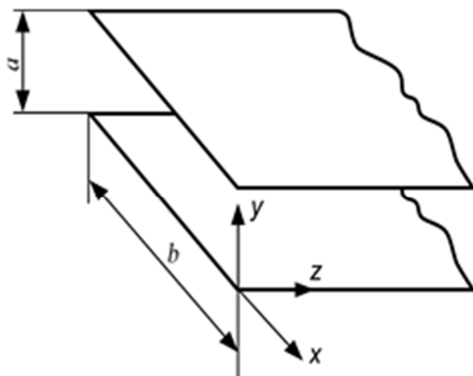


Fig. 1. The two-wire circuit, which consists of two ideally conducting planes.

Linear capacity and inductance of this line without taking into account edge effects they are determined by the relationships [8,9]:

$$C_0 = \epsilon_0 \frac{b}{a} \quad \text{and} \quad L_0 = \mu_0 \frac{a}{b}$$

Therefore with an increase in the length of line its total capacitance  $C_\Sigma = \epsilon_0 \frac{b}{a} z$  and summary inductance

$$L_\Sigma = \mu_0 \frac{a}{b} z \quad \text{increase proportional to its length.}$$

If we into the extended line place the plasma, charge carriers in which can move without the losses, and in the transverse direction pass through the plasma the current  $I$ , then charges, moving with the definite speed, will accumulate kinetic energy. Let us note that here are not examined technical questions, as and it is possible confined plasma between the planes of line how. In this case only fundamental questions, which are concerned transverse plasma resonance in the nonmagnetic plasma, are examined.

Since the transverse current density in this line is determined by the relationship

$$j = \frac{I}{bz} = nev,$$

that summary kinetic energy of the moving charges can be written down

$$W_{k\Sigma} = \frac{1}{2} \frac{m}{ne^2} abzj^2 = \frac{1}{2} \frac{m}{ne^2} \frac{a}{bz} I^2. \quad (3.1)$$

Relationship (3.1) connects the kinetic energy, accumulated in the line, with the square of current; therefore the coefficient, which stands in the right side of this relationship before the square of current, is the summary kinetic inductance of line.

$$L_{k\Sigma} = \frac{m}{ne^2} \cdot \frac{a}{bz} \quad (3.2)$$

Thus, the value

$$L_k = \frac{m}{ne^2} \quad (3.3)$$

presents the specific kinetic inductance of charges. This value was already previously introduced by another method (see relationship (2.4)). Relationship (3.3) is obtained for the case of the direct current, when current distribution is uniform.

Subsequently for the larger clarity of the obtained results, together with their mathematical idea, we will use the method of equivalent diagrams. The section, the lines examined, long  $dz$  can be represented in the form the equivalent diagram, shown in Fig. 2 (a).



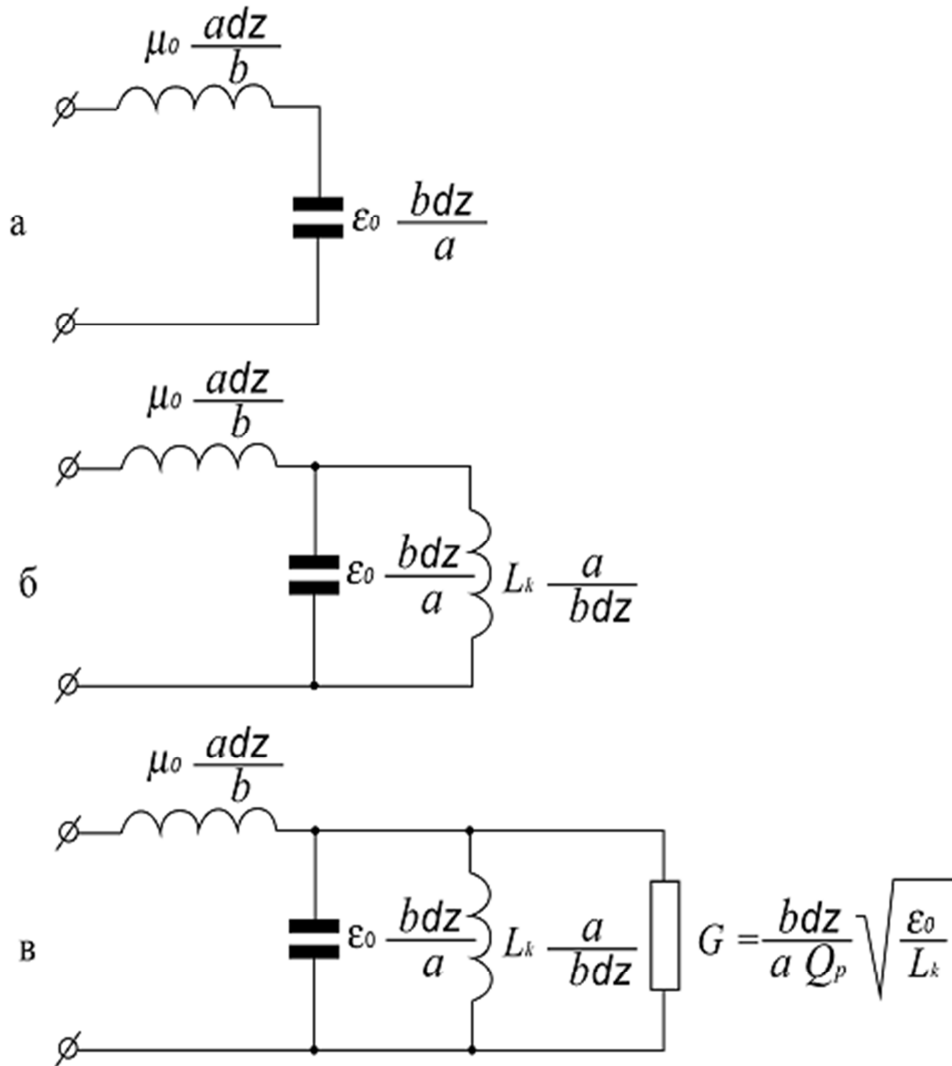


Fig. 2. a is the equivalent the schematic of the section of the two-wire circuit; б is the equivalent the schematic of the section of the two-wire circuit, filled with no dissipative plasma; B is the equivalent the schematic of the section of the two-wire circuit, filled with dissipative plasma.

From relationship (7.2) is evident that in contrast to  $C_{\Sigma}$  and  $L_{\Sigma}$  the value of  $L_{k\Sigma}$  with an increase in  $z$  does not increase, but it decreases. Connected this with the fact that with an increase in  $z$  a quantity of parallel-connected inductive elements grows.

The equivalent the schematic of the section of the line, filled with nondissipative plasma, it is shown in Fig. 2 б. Line itself in this case will be equivalent to parallel circuit with the lumped parameters:

$$C = \frac{\epsilon_0 b z}{a},$$

$$L = \frac{L_k a}{b z},$$

in series with which is connected the inductance

$$\mu_0 \frac{a d z}{b}.$$

But if we calculate the resonance frequency of this outline, then it will seem that this frequency generally not on what sizes depends, actually:

$$\omega_p^2 = \frac{1}{CL} = \frac{1}{\epsilon_0 L_k} = \frac{ne^2}{\epsilon_0 m}.$$

Is obtained the very interesting result, which speaks, that the resonance frequency macroscopic of the resonator examined does not depend on its sizes. Impression can be created, that this is plasma resonance, since. the obtained value of resonance frequency exactly corresponds to the value of this resonance. But it is known that the plasma resonance characterizes longitudinal waves in the long line they, while occur transverse waves. In the case examined the value of the phase speed in the direction  $z$  is equal to infinity and the wave vector  $\vec{k} = 0$ .

This result corresponds to the solution of system of equations (2.10) for the line with the assigned configuration. In this case the wave number is determined by the relationship:

$$k_z^2 = \frac{\omega^2}{c^2} \left( 1 - \frac{\omega_p^2}{\omega^2} \right), \tag{3.4}$$

and the group and phase speeds

$$v_g^2 = c^2 \left( 1 - \frac{\omega_p^2}{\omega^2} \right), \tag{3.5}$$

$$v_F^2 = \frac{c^2}{\left( 1 - \frac{\omega_p^2}{\omega^2} \right)}, \tag{3.6}$$

where  $c = \left( \frac{1}{\mu_0 \epsilon_0} \right)^{1/2}$  is speed of light in the vacuum.

For the present instance the phase speed of electromagnetic wave is equal to infinity, which corresponds to transverse resonance at the plasma frequency. Consequently, at each moment of time fields on distribution and currents in this line uniform and it does not depend on the coordinate  $z$ , but current in the planes of line in the direction of  $z$  is absent. This, from one side, it means that the inductance  $L_\Sigma$  will not have effects on electrodynamic processes in this line, but instead of the conducting planes can be used any planes or devices, which limit plasma on top and from below.

From relationships (3.4), (3.5) and (3.6) is evident that at the point of  $\omega = \omega_p$  occurs the transverse resonance with the infinite quality. With the presence of losses in the resonator will occur the damping, and in the long line in this case  $k_z \neq 0$ , and in the line will be extended the damped transverse wave, the direction of propagation of which will be normal to the direction of the motion of charges. It should be noted that the fact of existence of this resonance is not described by other authors.

Before to pass to the more detailed study of this problem, let us pause at the energy processes, which occur in the line in the case of the absence of losses examined.

The fields on the characteristic impedance of plasma, which gives the relation of the transverse components of electrical and magnetic, let us determine from the relationship

$$Z = \frac{E_y}{H_x} = \frac{\mu_0 \omega}{k_z} = Z_0 \left( 1 - \frac{\omega_p^2}{\omega^2} \right)^{-1/2},$$

where  $Z_0 = \sqrt{\frac{\mu_0}{\epsilon_0}}$  is characteristic resistance of vacuum.

The obtained value of  $Z$  is characteristic for the transverse electrical waves in the waveguides. It is evident that when  $\omega \rightarrow \omega_p$ , then  $Z \rightarrow \infty$ , and  $H_x \rightarrow 0$ . When  $\omega > \omega_p$  in the plasma there is electrical and magnetic component of field. The specific energy of these fields on it will be written down:

$$W_{E,H} = \frac{1}{2} \epsilon_0 E_{0y}^2 + \frac{1}{2} \mu_0 H_{0x}^2$$

Thus, the energy, concluded in the magnetic field, in  $\left( 1 - \frac{\omega_p^2}{\omega^2} \right)$  of times is less than the energy, concluded in the electric field. Let us note that this examination, which is traditional in the electrodynamics, is not complete, since. in this case is not taken into account one additional form of energy, namely kinetic energy of charge carriers. Occurs that fields on besides the waves of electrical and magnetic, that carry electrical and magnetic energy, in the plasma there exists even and the third - kinetic wave, which carries kinetic energy of current carriers. The specific energy of this wave is written:

$$W_k = \frac{1}{2} L_k j_0^2 = \frac{1}{2} \cdot \frac{1}{\omega^2 L_k} E_0^2 = \frac{1}{2} \epsilon_0 \frac{\omega_p^2}{\omega^2} E_0^2.$$

Consequently, the total specific energy of wave is written as

$$W_{E,H,j} = \frac{1}{2} \epsilon_0 E_{0y}^2 + \frac{1}{2} \mu_0 H_{0x}^2 + \frac{1}{2} L_k j_0^2.$$

Thus, for finding the total energy, by the prisoner per unit of volume of plasma, calculation only fields on  $E$  and  $H$  it is insufficient.

At the point  $\omega = \omega_p$  are carried out the relationship:

$$\begin{aligned} W_H &= 0 \\ W_E &= W_k \end{aligned}$$

i.e. magnetic field in the plasma is absent, and plasma presents macroscopic electromechanical resonator with the infinite quality,  $\omega_p$  resounding at the frequency.

Since with the frequencies  $\omega > \omega_p$  the wave, which is extended in the plasma, it bears on itself three forms of the energy: electrical, magnetic and kinetic, then this wave can be named elektromagnetokinetic wave. Kinetic wave is the wave

of the current density  $\vec{j} = \frac{1}{L_k} \int \vec{E} dt$ . This wave is moved

with respect to the electrical wave the angle  $\frac{\pi}{2}$ .

Until now considered physically unrealizable case where there are no losses in the plasma, which corresponds to an infinite quality factor plasma resonator. If losses are located, moreover completely it does not have value, by what physical processes such losses are caused, then the quality of plasma resonator will be finite quantity. For this case of Maxwell's equation they will take the form:

$$\begin{aligned} \text{rot } \vec{E} &= -\mu_0 \frac{\partial \vec{H}}{\partial t}, \\ \text{rot } \vec{H} &= \sigma_{p,ef} \vec{E} + \epsilon_0 \frac{\partial \vec{E}}{\partial t} + \frac{1}{L_k} \int \vec{E} dt. \end{aligned} \quad (3.7)$$

The presence of losses is considered by the term  $\sigma_{p,ef} \vec{E}$ , and, using near the conductivity of the index of  $ef$ , it is thus emphasized that us does not interest very mechanism of losses, but only very fact of their existence interests. The value of  $\sigma_{ef}$  determines the quality of plasma resonator. For measuring  $\sigma_{ef}$  should be selected the section of line by the length of  $z_0$ , whose value is considerably lower than the wavelength in the plasma. This section will be equivalent to outline with the lumped parameters:

$$C = \epsilon_0 \frac{bz_0}{a}, \quad (3.8)$$

$$L = L_k \frac{a}{bz_0}, \quad (3.9)$$

$$G = \sigma_{p,ef} \frac{bz_0}{a}, \quad (3.10)$$

where  $G$  is conductivity, connected in parallel of  $C$  and  $L$ .

Conductivity and quality in this outline enter into the relationship:

$$G = \frac{1}{Q_p} \sqrt{\frac{C}{L}},$$

from where, taking into account (3.8 - 3.10), we obtain

$$\sigma_{p,ef} = \frac{1}{Q_p} \sqrt{\frac{\epsilon_0}{L_k}} \quad (3.11)$$

Thus, measuring its own quality plasma of the resonator examined, it is possible to determine  $\sigma_{p,ef}$ . Using (3.2) and (3.11) we will obtain

$$\begin{aligned} \text{rot } \vec{E} &= -\mu_0 \frac{\partial \vec{H}}{\partial t}, \\ \text{rot } \vec{H} &= \frac{1}{Q_p} \sqrt{\frac{\epsilon_0}{L_k}} \vec{E} + \epsilon_0 \frac{\partial \vec{E}}{\partial t} + \frac{1}{L_k} \int \vec{E} dt. \end{aligned} \quad (3.12)$$

The equivalent the schematic of this line, filled with dissipative plasma, is represented in Fig. 2 B.

Let us examine the solution of system of equations (3.12) at the point  $\omega = \omega_p$ , in this case, since

$$\epsilon_0 \frac{\partial \vec{E}}{\partial t} + \frac{1}{L_k} \int \vec{E} dt = 0,$$

we obtain

$$\begin{aligned} \text{rot } \vec{E} &= -\mu_0 \frac{\partial \vec{H}}{\partial t}, \\ \text{rot } \vec{H} &= \frac{1}{Q_p} \sqrt{\frac{\epsilon_0}{L_k}} \vec{E}. \end{aligned}$$

These relationships determine wave processes at the point of resonance.

If losses in the plasma, which fills line are small, and strange current source is connected to the line, then it is possible to assume:

$$\begin{aligned} \text{rot } \vec{E} &\cong 0, \\ \frac{1}{Q_p} \sqrt{\frac{\epsilon_0}{L_k}} \vec{E} + \epsilon_0 \frac{\partial \vec{E}}{\partial t} + \frac{1}{L_k} \int \vec{E} dt &= \vec{j}_{CT}, \end{aligned} \quad (3.13)$$

where  $\vec{j}_{CT}$  is density of strange currents.

After integrating (3.13) with respect to the time and after dividing both parts to  $\epsilon_0$ , we will obtain

$$\omega_p^2 \vec{E} + \frac{\omega_p}{Q_p} \cdot \frac{\partial \vec{E}}{\partial t} + \frac{\partial^2 \vec{E}}{\partial t^2} = \frac{1}{\epsilon_0} \cdot \frac{\partial \vec{j}_{CT}}{\partial t}. \quad (3.14)$$

If we relationship (3.14) integrate over the surface of normal to the vector  $\vec{E}$  and to introduce the electric flux  $\Phi_E = \int \vec{E} d\vec{S}$ , we will obtain:

$$\omega_p^2 \Phi_E + \frac{\omega_p}{Q_p} \cdot \frac{\partial \Phi_E}{\partial t} + \frac{\partial^2 \Phi_E}{\partial t^2} = \frac{1}{\epsilon_0} \cdot \frac{\partial I_{CT}}{\partial t}, \quad (3.15)$$

where  $I_{CT}$  is strange current.

Equation (3.15) is the equation of harmonic oscillator with the right side, characteristic for the two-level laser [14]. If the source of excitation was opened, then relationship (3.14) presents “cold” laser resonator, in which the fluctuations will attenuate exponentially

$$\Phi_E(t) = \Phi_E(0) e^{i\omega_p t} \cdot e^{-\frac{\omega_p}{2Q_p} t},$$

i.e. the macroscopic electric flux  $\Phi_E(t)$  will oscillate with the frequency  $\omega_p$ , relaxation time in this case is determined by the relationship:

$$\tau = \frac{2Q_p}{\omega_p}.$$

The problem of developing of laser consists to now only in the skill excite this resonator.

If resonator is excited by strange currents, then this resonator presents band-pass filter with the resonance frequency to equal plasma frequency and the passband

$$\Delta\omega = \frac{\omega_p}{2Q_p}.$$

Another important practical application of transverse plasma resonance is possibility its use for warming-up and diagnostics of plasma. If the quality of plasma resonator is great, then can be obtained the high levels of electrical fields on, and it means high energies of charge carriers.

#### 4. Dielectrics

In the existing literature there are no indications that the kinetic inductance of charge carriers plays some role in the electrodynamic processes in the dielectrics. This not thus. This parameter in the electrodynamic processes in dielectrics plays not less important role, than in the electrodynamic processes in conductors. Let us examine the simplest case, when oscillating processes in atoms or molecules of dielectric obey the law of mechanical oscillator [8]. Let us write down the equation of motion

$$\left(\frac{\beta}{m} - \omega^2\right) \vec{r}_m = \frac{e}{m} \vec{E}, \quad (4.1)$$

where  $\vec{r}_m$  is deviation of charges from the position of equilibrium,  $\beta$  is coefficient of elasticity, which characterizes the elastic electrical binding forces of charges in the atoms and the molecules. Introducing the resonance frequency of the bound charges

$$\omega_0 = \frac{\beta}{m},$$

we obtain from (4.1)

$$r_m = -\frac{e E}{m(\omega^2 - \omega_0^2)}. \quad (4.2)$$

Is evident that in relationship (4.2) as the parameter is present the natural vibration frequency, into which enters the mass of charge. This speaks, that the inertia properties of the being varied charges will influence oscillating processes in the atoms and the molecules.

Since the general current density on medium consists of the bias current and conduction current

$$\text{rot} \vec{H} = \vec{j}_\Sigma = \varepsilon_0 \frac{\partial \vec{E}}{\partial t} + ne\vec{v},$$

that, finding the speed of charge carriers in the dielectric as the derivative of their displacement through the coordinate

$$\vec{v} = \frac{\partial r_m}{\partial t} = -\frac{e}{m(\omega^2 - \omega_0^2)} \frac{\partial \vec{E}}{\partial t},$$

from relationship (4.2) we find

$$\text{rot} \vec{H} = \vec{j}_\Sigma = \varepsilon_0 \frac{\partial \vec{E}}{\partial t} - \frac{1}{L_{kd}(\omega^2 - \omega_0^2)} \frac{\partial \vec{E}}{\partial t}. \quad (4.3)$$

Let us note that the value

$$L_{kd} = \frac{m}{ne^2}$$

presents the kinetic inductance of the charges, entering the constitution of atom or molecules of dielectrics, when to consider charges free. Therefore relationship (4.3) it is possible to rewrite

$$\text{rot} \vec{H} = \vec{j}_\Sigma = \varepsilon_0 \left(1 - \frac{1}{\varepsilon_0 L_{kd}(\omega^2 - \omega_0^2)}\right) \frac{\partial \vec{E}}{\partial t}. \quad (4.4)$$

Since the value

$$\frac{1}{\varepsilon_0 L_{kd}} = \omega_{pd}^2$$

it represents the plasma frequency of charges in atoms and molecules of dielectric, if we consider these charges free, then relationship (4.4) takes the form:

$$\text{rot} \vec{H} = \vec{j}_\Sigma = \varepsilon_0 \left(1 - \frac{\omega_{pd}^2}{(\omega^2 - \omega_0^2)}\right) \frac{\partial \vec{E}}{\partial t}. \quad (4.5)$$

To appears temptation to name the value

$$\varepsilon^*(\omega) = \varepsilon_0 \left(1 - \frac{\omega_{pd}^2}{(\omega^2 - \omega_0^2)}\right) \quad (4.6)$$

by the depending on the frequency dielectric constant of dielectric. But this, as in the case conductors, cannot be made, since this is the composite parameter, which includes now those not already three depending on the frequency of the parameter: the dielectric constant of vacuum, the natural frequency of atoms or molecules and plasma frequency for the charge carriers, entering their composition.

Let us examine two limiting cases:

1. If  $\omega \ll \omega_0$  then from (4.5) we obtain

$$\text{rot} \vec{H} = \vec{j}_\Sigma = \varepsilon_0 \left(1 + \frac{\omega_{pd}^2}{\omega_0^2}\right) \frac{\partial \vec{E}}{\partial t}. \quad (4.7)$$

In this case the coefficient, confronting the derivative, does not depend on frequency, and it presents the static dielectric constant of dielectric. As we see, it depends on the natural frequency of oscillation of atoms or molecules and on plasma frequency. This result is intelligible. Frequency in this case proves to be such low that the charges manage to follow the field and their inertia properties do not influence electrodynamic processes. In this case the bracketed expression in the right side of relationship (4.7) presents the static dielectric constant of dielectric. As we see, it depends on

the natural frequency of oscillation of atoms or molecules and on plasma frequency. Hence immediately we have a prescription for creating the dielectrics with the high dielectric constant. In order to reach this, should be in the assigned volume of space packed a maximum quantity of molecules with maximally soft connections between the charges inside molecule itself.

2. The case, when  $\omega \gg \omega_0$ , is exponential. In this case

$$\text{rot}\vec{H} = \vec{j}_\Sigma = \epsilon_0 \left( 1 - \frac{\omega_{pd}^2}{\omega^2} \right) \frac{\partial \vec{E}}{\partial t}$$

and dielectric became conductor (plasma) since the obtained relationship exactly coincides with the equation, which describes plasma.

One cannot fail to note the circumstance that in this case again nowhere was used this concept as polarization vector, but examination is carried out by the way of finding the real currents in the dielectrics on the basis of the equation of motion of charges in these media. In this case as the parameters are used the electrical characteristics of the media, which do not depend on frequency.

From relationship (4.5) is evident that in the case of fulfilling the equality  $\omega = \omega_0$ , the amplitude of fluctuations is equal to infinity. This indicates the presence of resonance at this point. The infinite amplitude of fluctuations occurs because of the fact that they were not considered losses in the resonance system, in this case its quality was equal to infinity. In a certain approximation it is possible to consider that lower than the point indicated we deal concerning the dielectric, whose dielectric constant is equal to its static value. Higher than this point we deal already actually concerning the metal, whose density of current carriers is equal to the density of atoms or molecules in the dielectric.

Now it is possible to examine the question of why dielectric prism decomposes polychromatic light into monochromatic components or why rainbow is formed. So that this phenomenon would occur, it is necessary to have the frequency dispersion of the phase speed of electromagnetic waves in the medium in question. If we to relationship (4.5) add the Maxwell first equation, then we will obtain:

$$\begin{aligned} \text{rot}\vec{E} &= -\mu_0 \frac{\partial \vec{H}}{\partial t} \\ \text{rot}\vec{H} &= \epsilon_0 \left( 1 - \frac{\omega_{pd}^2}{(\omega^2 - \omega_0^2)} \right) \frac{\partial \vec{E}}{\partial t} \end{aligned}$$

from where we immediately find the wave equation:

$$\nabla^2 \vec{E} = \mu_0 \epsilon_0 \left( 1 - \frac{\omega_{pd}^2}{\omega^2 - \omega_0^2} \right) \frac{\partial^2 \vec{E}}{\partial t^2}$$

If one considers that

$$\mu_0 \epsilon_0 = \frac{1}{c^2}$$

where  $C$  is speed of light, then no longer will remain doubts about the fact that with the propagation of electromagnetic waves in the dielectrics the frequency dispersion of phase speed will be observed. In the formation of this dispersion it will participate immediately three, which do not depend on the frequency, physical quantities: the self-resonant frequency of atoms themselves or molecules, the plasma frequency of charges, if we consider it their free, and the dielectric constant of vacuum.

Now let us show, where it is possible to be mistaken, if with the solution of the examined problem of using a concept of polarization vector. Let us introduce this polarization vector

$$\vec{P} = -\frac{ne^2}{m} \cdot \frac{1}{(\omega^2 - \omega_0^2)} \vec{E}$$

Its dependence on the frequency, is connected with the presence of mass in the charges, entering the constitution of atom and molecules of dielectrics. The inertness of charges is not allowed for this vector, following the electric field, to reach that value, which it would have in the permanent fields. Since the electrical induction is determined by the relationship:

$$\vec{D} = \epsilon_0 \vec{E} + \vec{P} \vec{E} = \epsilon_0 \vec{E} - \frac{ne^2}{m} \cdot \frac{1}{(\omega^2 - \omega_0^2)} \vec{E}, \quad (4.8)$$

that, introduced thus, it depends on frequency.

If this induction was introduced into the Maxwell second equation, then it signs the form:

$$\text{rot}\vec{H} = j_\Sigma = \epsilon_0 \frac{\partial \vec{E}}{\partial t} + \frac{\partial \vec{P}}{\partial t}$$

or

$$\text{rot}\vec{H} = j_\Sigma = \epsilon_0 \frac{\partial \vec{E}}{\partial t} - \frac{ne^2}{m} \frac{1}{(\omega^2 - \omega_0^2)} \frac{\partial \vec{E}}{\partial t} \quad (4.9)$$

where  $\vec{j}_\Sigma$  is the summed current, which flows through the model. In expression (4.9) the first member of right side presents bias current in the vacuum, and the second - current, connected with the presence of bound charges in atoms or molecules of dielectric. In this expression again appeared the specific kinetic inductance of the charges, which participate in the oscillating process of

$$L_{kd} = \frac{m}{ne^2}$$

This kinetic inductance determines the inductance of bound charges. Taking into account this relationship (4.9) it is possible to rewrite

$$\text{rot}\vec{H} = j_\Sigma = \epsilon_0 \frac{\partial \vec{E}}{\partial t} - \frac{1}{L_{kd}} \frac{1}{(\omega^2 - \omega_0^2)} \frac{\partial \vec{E}}{\partial t}$$

Obtained expression exactly coincides with relationship

(4.3). Consequently, the eventual result of examination by both methods coincides, and there are no claims to the method from a mathematical point of view. But from a physical point of view, and especially in the part of the awarding to the parameter, introduced in accordance with relationship (4.8) of the designation of electrical induction, are large claims, which we discussed. Is certain, this not electrical induction, but the certain composite parameter. But, without having been dismantled at the essence of a question, all, until now, consider that the dielectric constant of dielectrics depends on frequency. In the essence, physically substantiated is the introduction to electrical induction in the dielectrics only in the static electric fields.

Let us show that the equivalent the schematic of dielectric presents the sequential resonant circuit, whose inductance is the kinetic inductance  $L_{kd}$ , and capacity is equal to the static dielectric constant of dielectric minus the capacity of the equal dielectric constant of vacuum. In this case outline itself proves to be that shunted by the capacity, equal to the specific dielectric constant of vacuum. For the proof of this let us examine the sequential oscillatory circuit, when the inductance  $L$  and the capacity  $C$  are connected in series.

The connection between the current  $I_C$ , which flows through the capacity  $C$ , and the voltage  $U_C$ , applied to it, is determined by the relationships:

$$U_C = \frac{1}{C} \int I_C dt$$

and

$$I_C = C \frac{dU_C}{dt} . \quad (4.10)$$

This connection will be written down for the inductance:

$$I_L = \frac{1}{L} \int U_L dt$$

and

$$U_L = L \frac{dI_L}{dt} .$$

If the current, which flows through the series circuit, changes according to the law  $I = I_0 \sin \omega t$ , then a voltage drop across inductance and capacity they are determined by the relationships

$$U_L = \omega L I_0 \cos \omega t$$

and

$$U_C = -\frac{1}{\omega C} I_0 \cos \omega t ,$$

and total stress applied to the outline is equal

$$U_\Sigma = \left( \omega L - \frac{1}{\omega C} \right) I_0 \cos \omega t .$$

In this relationship the value, which stands in the brackets, presents the reactance of sequential resonant circuit, which depends on frequency. The stresses, generated on the capacity and the inductance, are located in the reversed phase, and, depending on frequency, outline can have the inductive, the whether capacitive reactance. At the point of resonance the summary reactance of outline is equal to zero.

It is obvious that the connection between the total voltage applied to the outline and the current, which flows through the outline, will be determined by the relationship

$$I = -\frac{1}{\omega \left( \omega L - \frac{1}{\omega C} \right)} \frac{\partial U_\Sigma}{\partial t} . \quad (4.11)$$

The resonance frequency of outline is determined by the relationship

$$\omega_0 = \frac{1}{\sqrt{LC}} ,$$

therefore let us write down

$$I = \frac{C}{\left( 1 - \frac{\omega^2}{\omega_0^2} \right)} \frac{\partial U_\Sigma}{\partial t} . \quad (4.12)$$

Comparing this expression with relationship (4.10) it is not difficult to see that the sequential resonant circuit, which consists of the inductance  $L$  and capacity  $C$ , it is possible to present to the capacity the form dependent on the frequency

$$C(\omega) = \frac{C}{\left( 1 - \frac{\omega^2}{\omega_0^2} \right)} . \quad (4.13)$$

This idea does not completely mean that the inductance is somewhere lost. Simply it enters into the resonance frequency of the outline  $\omega_0$ . Relationship (4.12) this altogether only the mathematical form of the record of relationship (4.11). Consequently, this is  $C(\omega)$  the certain composite mathematical parameter, which is not the capacity of outline.

Relationship (4.11) can be rewritten and differently:

$$I = -\frac{1}{L(\omega^2 - \omega_0^2)} \frac{\partial U_\Sigma}{\partial t}$$

and to consider that

$$C(\omega) = -\frac{1}{L(\omega^2 - \omega_0^2)} . \quad (4.14)$$

Is certain, the parameter  $C(\omega)$ , introduced in accordance

with relationships (4.13) and (4.14) no to capacity refers.

Let us examine relationship (9.12) for two limiting cases:

1. When  $\omega \ll \omega_0$ , we have

$$I = C \frac{\partial U_{\Sigma}}{\partial t}.$$

This result is intelligible, since at the low frequencies the reactance of the inductance, connected in series with the capacity, is considerably lower than the capacitive and it is possible not to consider it.

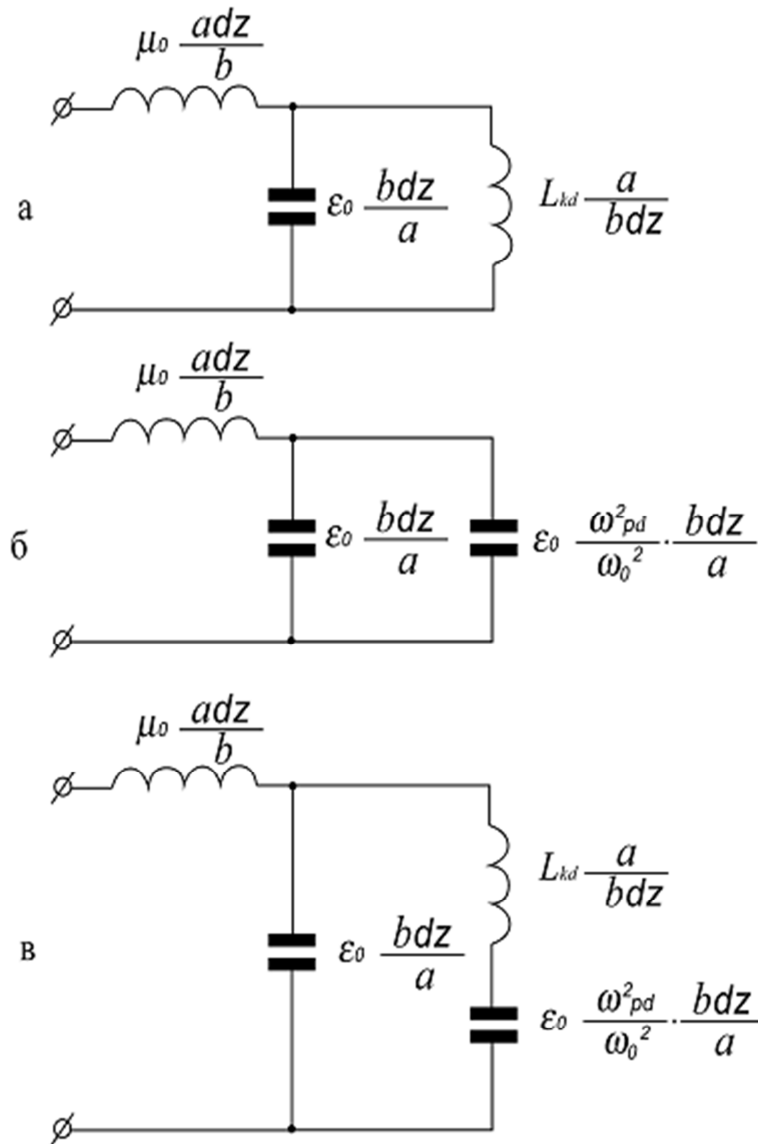


Fig. 3. a is the equivalent schematic of the section of the line, filled with dielectric, for the case  $\omega \gg \omega_0$ ; b is the equivalent schematic of the section of line for the case  $\omega \ll \omega_0$ ; B is the equivalent schematic of the section of line for entire frequency band.

The equivalent schematic of the dielectric, located between the planes of long line is shown in Fig. 3.

2. For the case, when  $\omega \gg \omega_0$ , we have

$$I = -\frac{1}{\omega^2 L} \frac{\partial U_{\Sigma}}{\partial t} \tag{4.15}$$

we obtain from (4.15)

$$\frac{\partial U_{\Sigma}}{\partial t} = -\omega^2 \int U_{\Sigma} dt,$$

$$I_L = \frac{1}{L} \int U_{\Sigma} dt.$$

Taking into account that for the harmonic signal

In this case the reactance of capacity is considerably less than in inductance and chain has inductive reactance.

The carried out analysis speaks, that is in practice very difficult to distinguish the behavior of resonant circuits of the inductance or of the capacity. In order to understand the true composition of the chain being investigated it is necessary to remove the amplitude and phase response of this chain in the range of frequencies. In the case of resonant circuit this dependence will have the typical resonance nature, when on both sides resonance the nature of reactance is different. However, this does not mean that real circuit elements: capacity or inductance depend on frequency.

In Fig. 3 a and 5 б are shown two limiting cases. In the first case, when  $\omega \gg \omega_0$ , dielectric according to its properties corresponds to conductor, in the second case, when  $\omega \ll \omega_0$ , it corresponds to the dielectric, which possesses the static

$$\text{dielectric constant } \varepsilon = \varepsilon_0 \left( 1 + \frac{\omega_{pd}^2}{\omega_0^2} \right).$$

Thus, it is possible to make the conclusion that the introduction, the depending on the frequency dielectric constants of dielectrics, are physical and terminological error. If the discussion deals with the dielectric constant of dielectrics, with which the accumulation of potential energy is connected, then the discussion can deal only with the static permeability. And precisely this parameter as the constant, which does not depend on the frequency, enters into all relationships, which characterize the electrodynamic characteristics of dielectrics.

The most interesting results of applying such new approaches occur precisely for the dielectrics. In this case each connected pair of charges presents the separate unitary unit with its individual characteristics and its participation in the processes of interaction with the electromagnetic field (if we do not consider the connection between the separate pairs) strictly individually. Certainly, in the dielectrics not all dipoles have different characteristics, but there are different groups with similar characteristics, and each group of bound charges with the identical characteristics will resound at its frequency. Moreover the intensity of absorption, and in the excited state and emission, at this frequency will depend on a relative quantity of pairs of this type. Therefore the partial coefficients, which consider their statistical weight in this process, can be introduced. Furthermore, these processes will influence the anisotropy of the dielectric properties of molecules themselves, which have the specific electrical orientation in crystal lattice. By these circumstances is determined the variety of resonances and their intensities, which is observed in the dielectric media. The lines of absorption or emission, when there is a electric coupling between the separate groups of emitters, acquire even more complex structure. In this case the lines can be converted into the strips. Such individual approach to each separate type of the connected pairs of charges could not be realized within the framework earlier than the existing approaches.

Should be still one important circumstance, which did not up to now obtain proper estimation. With the examination of processes in the material media, which they are both conductors and dielectrics in all relationships together with the

dielectric and magnetic constant figures the kinetic inductance of charges. This speaks, that the role of this parameter with the examination of processes in the material media has not less important role, than dielectric and magnetic constant. This is for the first time noted in a number the already mentioned sources, including in the recently published article [11].

## 5. Brief Conclusions

It seems in effect improbable what a large quantity of well-known physicists is, beginning with the Drudes, Vula and Heaviside [1,15] and concluding By akhiezerom, by Tamm, Ginsburg and Landau [2-5], they completed such elementary and at the same time blunder, which served as basis for the development of the whole it obliged in contemporary physics, in which is examined the dispersion of the dielectric and magnetic constant of material media. But, nevertheless, this so, and this work convincingly proves, that this error was perfected and requires its correction. But this indicates not only the revision of the ideological part of such approaches, but also the introduction of corrections into a huge quantity of works, reference books and fundamental monographs. And this work sooner or later it will arrive to accomplish to the present generation of scientists. The error indicated led also to the fact that in the field of the sight of physicists did not fall this interesting physical phenomenon, as the transverse plasma resonance in the nonmagnetized plasma, which can have important technical applications.

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